

A tutorial on conducting portfolio optimization

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Saturday, August 02, 2014

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1 Start up

```
inslib <- function(x){  
  x <-as.character(substitute(x))  
  if(!x %in% rownames(installed.packages()))  
    {install.packages(x,repos="http://cran.stat.ucla.edu")}  
  eval(parse(text=paste("library(",x,")",sep="")))}  
  
inslib("quadprog")  
inslib("xts")  
inslib("Rglpk")  
inslib("corpcor")  
source("mvo.constrained.r")  
source("efront.constrained.r")  
source("barplot.wts.r")  
source("constraint.sets.r")  
load("crsp.short.Rdata")
```

```

n.stocks <- 5
names(midcap.ts)

## [1] "MAT"      "EMN"      "LEG"      "AAPL"      "UTR"       "HB"        "BNK"
## [8] "APA"       "LNCR"     "BMET"     "DBD"       "FAST"      "AF"        "CPWR"
## [15] "EC"        "SNV"      "HSY"      "TXT"       "APCC"      "LXK"       "market"
## [22] "t90"

names(smallcap.ts)

## [1] "MODI"     "MGF"      "MEE"      "FCEL"      "OII"       "SEB"       "RML"
## [8] "AEOS"     "BRC"      "CTC"      "TNL"       "IBC"       "KWD"       "TOPP"
## [15] "RARE"     "HAR"      "BKE"      "GG"        "GYMB"      "KRON"      "market"
## [22] "t90"

names(largecap.ts)

## [1] "AMAT"     "AMGN"     "CAT"      "DD"        "G"         "GENZ"      "GM"
## [8] "HON"       "KR"        "LLTC"     "MSFT"      "ORCL"      "PG"        "PHA"
## [15] "SO"        "TXN"      "UTX"      "WM"        "WYE"       "YHOO"      "market"
## [22] "t90"

returns.ts = midcap.ts[,1:n.stocks]
returns = coredata(midcap.ts[,1:n.stocks])
sum=1
mu.target=0.02
w.initial=rep(1/n.stocks,n.stocks)
toc=0.3
upper=rep(0.5,n.stocks)
lower=rep(0,n.stocks)

set.seed(1234)
group=c(sample(1:2,n.stocks,replace=T))
upper.group=c(0.5,0.5)
lower.group=c(-0.5,0.5)
ptc=0.001
digits=4
wts.only=T
mu.min = NULL
mu.max = NULL
rf = .003
npoints = 20
wts.plot = T
printout = F
bar.ylim = c(-1,4)

```

Initial parameter values on constraints:

```

list.arg <- list(
  sum=sum,
  mu.target=mu.target,

```

```

group=group,
upper.group=upper.group,
lower.group=lower.group,
upper=upper,
lower=lower,
toc=toc,
w.initial=w.initial,
ptc=ptc)
list.arg

```

```

## $sum
## [1] 1
##
## $mu.target
## [1] 0.02
##
## $group
## [1] 1 2 2 2 2
##
## $upper.group
## [1] 0.5 0.5
##
## $lower.group
## [1] -0.5 0.5
##
## $upper
## [1] 0.5 0.5 0.5 0.5 0.5
##
## $lower
## [1] 0 0 0 0 0
##
## $toc
## [1] 0.3
##
## $w.initial
## [1] 0.2 0.2 0.2 0.2 0.2
##
## $ptc
## [1] 0.001

```

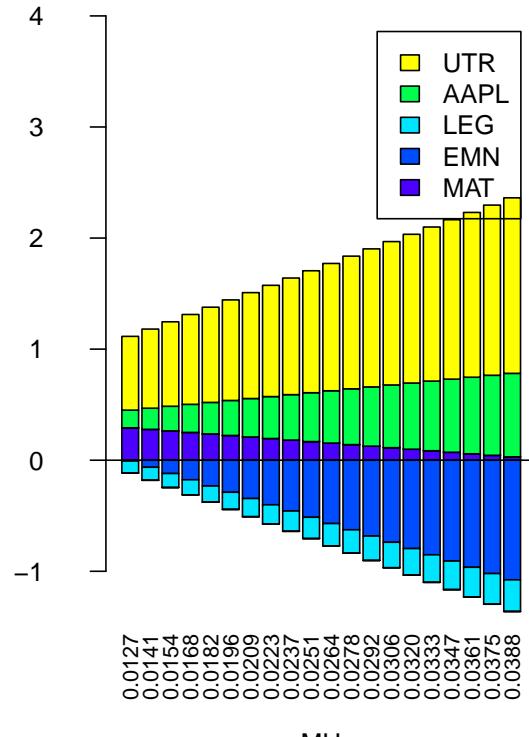
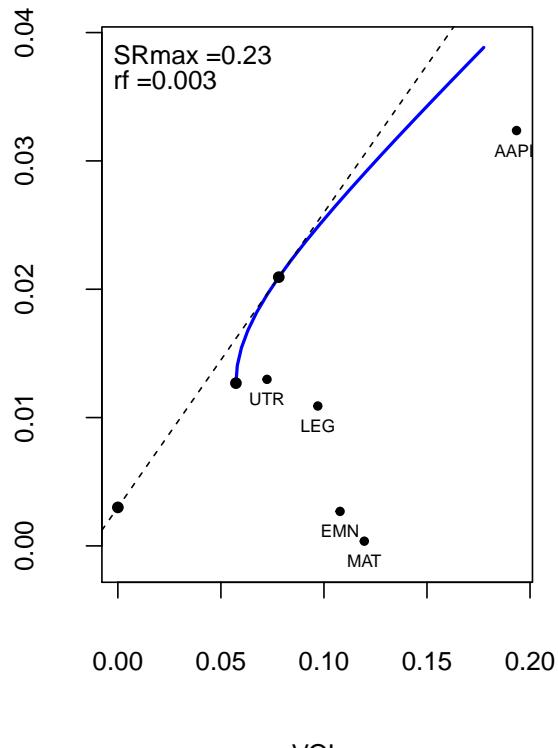
2 Null constraint

```

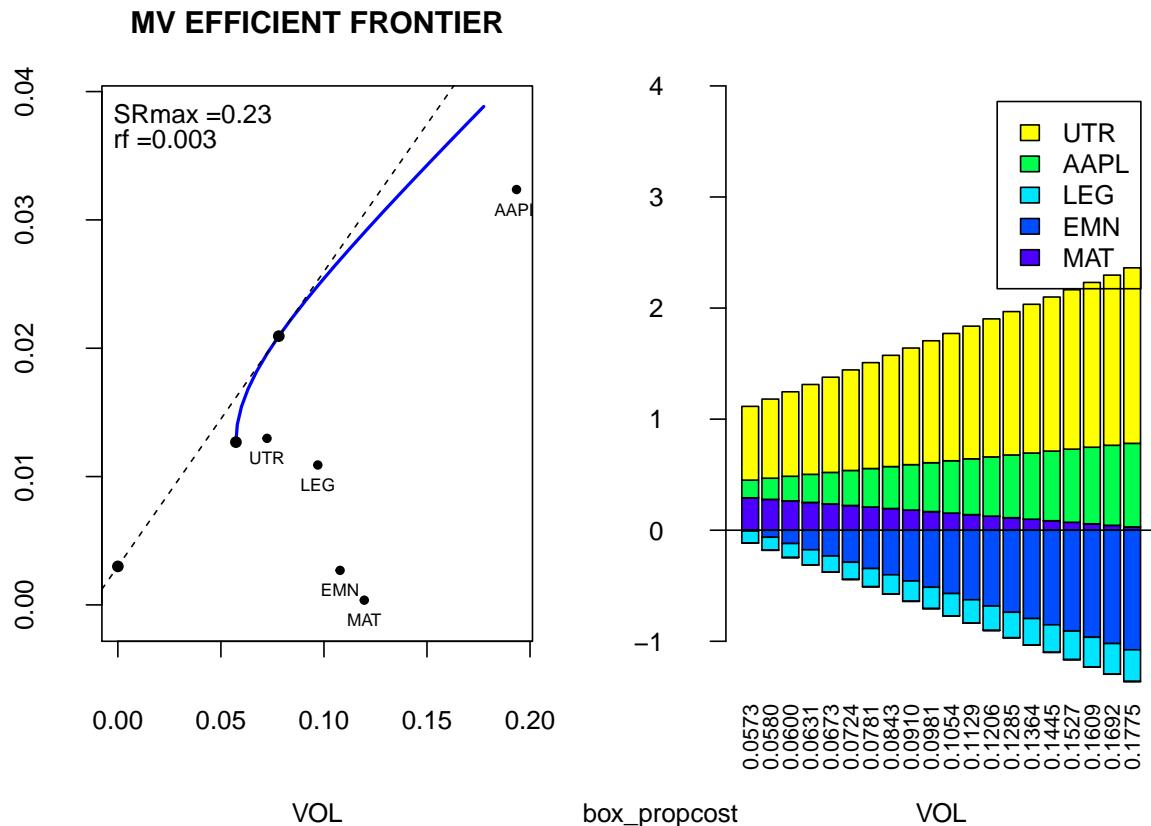
cset=NULL # gmv
#wt plot using MU on horizontal
efrontPlot(returns, cset, rf = .003, npoints = 20,wts.plot = T,
           bar.ylim = c(-1,4),list.arg=list.arg, wts.xlab="MU")

```

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```
#wt plot using VOL on horizontal
efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
           bar.ylim = c(-1,4), list.arg=list.arg, wts.xlab="VOL")
mtext(paste(clist,collapse="_"), side=1, line=5)
```



3 Full investment constraint

```

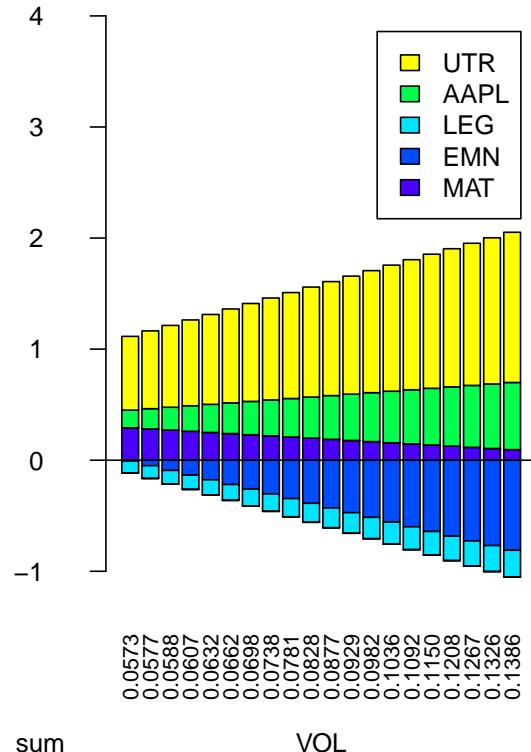
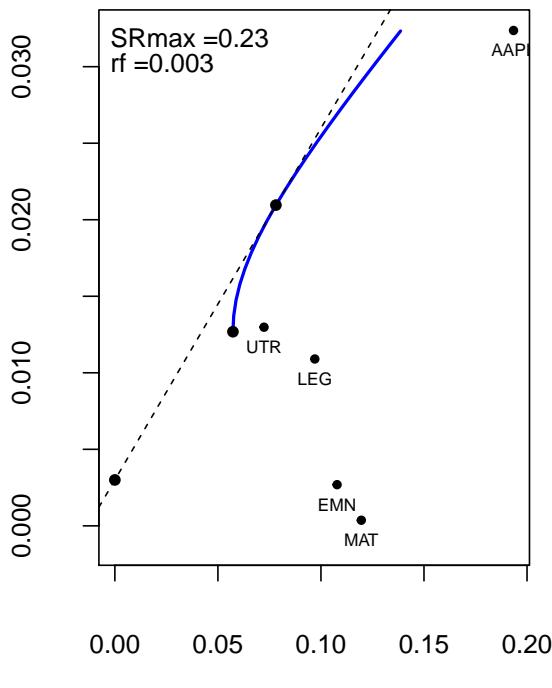
clist <- c("sum")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg=list.arg)

## sum

efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
           bar.ylim = c(-1,4), list.arg=list.arg)
mtext(paste(clist, collapse="_"), side=1, line=5)

```

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Full investment and long only constraints =====

```
clist <- c("sum", "lo")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg=list.arg)
```

```
## sum
## lo

gmv(returns, cset=cset, wts.only=T, digits=4)
```

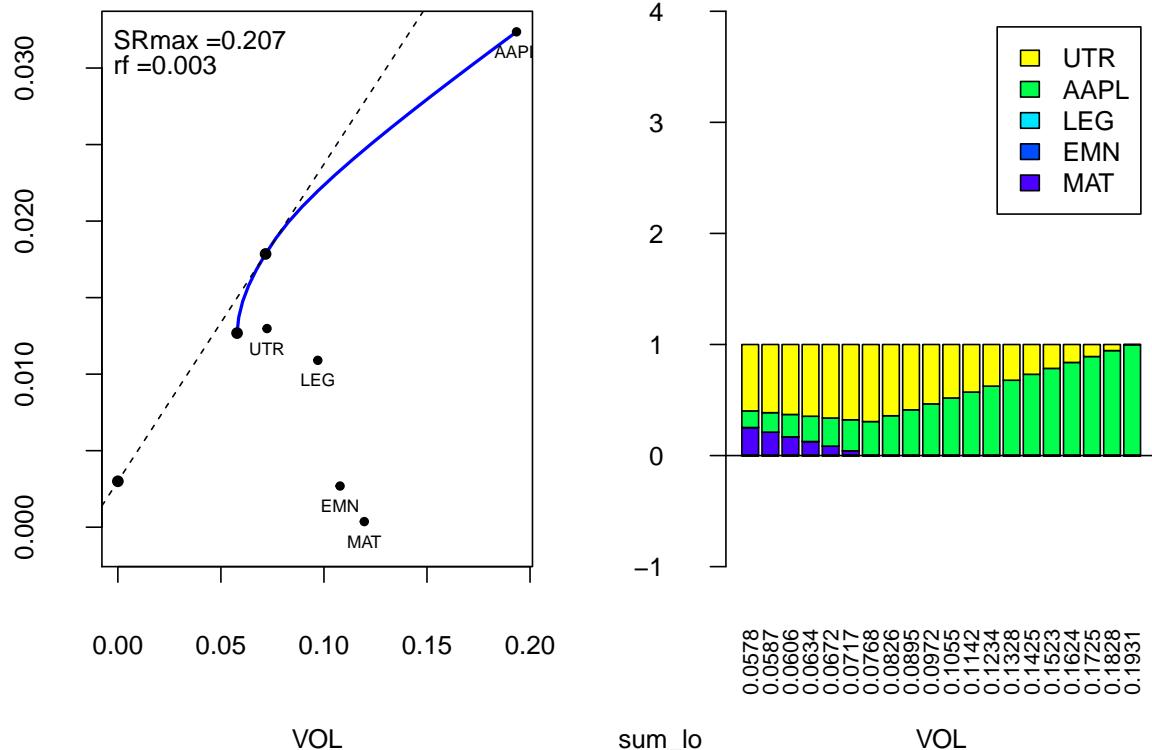
```
## $WTS
##      MAT      EMN      LEG      AAPL      UTR
## 0.2622 0.0000 0.0000 0.1433 0.5945
##
## $MU.PORT
## [1] 0.0124
##
## $SD.PORT
## [1] 0.0578
```

```

efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
           bar.ylim = c(-1,4), list.arg=list.arg)
mtext(paste(clist,collapse=" ")), side=1, line=5)

```

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Full investment, long only and box constraints =====

```

clist <- c("sum", "lo", "box")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg=list.arg)

## sum
## lo
## box

gmv(returns, cset=cset, wts.only=T, digits=4)

## $WTS
##      MAT      EMN      LEG     AAPL      UTR
## 0.3008 0.0372 0.0000 0.1620 0.5000
##
## $MU.PORT
## [1] 0.0119

```

```

##  

## $SD.PORT  

## [1] 0.0585  

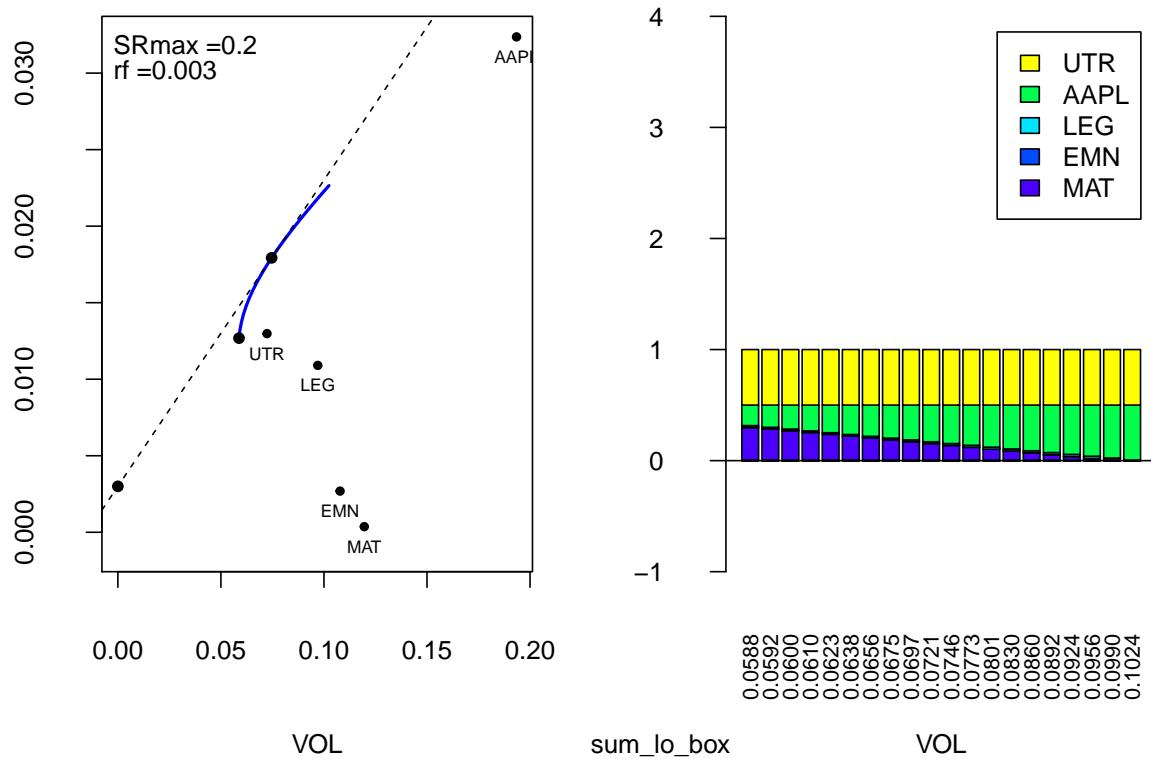
efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,  

           bar.ylim = c(-1,4), list.arg=list.arg)  

mtext(paste(clist,collapse=" " ),side=1,line=5)

```

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Full investment, long only and group constraints =====

```

clist <- c("sum", "lo", "groups")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg=list.arg)

```

```

## sum
## lo
## groups

gmv(returns, cset=cset, wts.only=T, digits=4)

```

```

## $WTS
##      MAT      EMN      LEG      AAPL      UTR

```

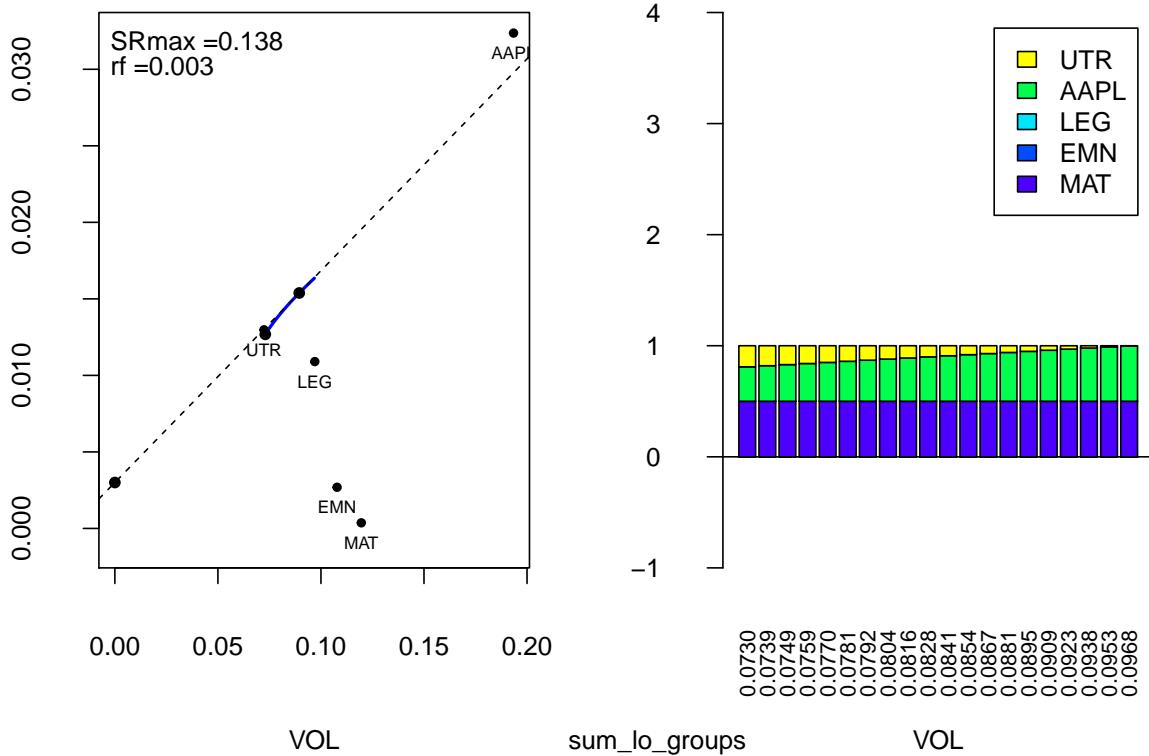
```

## 0.5000 0.0000 0.0000 0.1574 0.3426
##
## $MU.PORT
## [1] 0.0097
##
## $SD.PORT
## [1] 0.0657

efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
           bar.ylim = c(-1,4), list.arg=list.arg)
mtext(paste(clist, collapse=" " ), side=1, line=5)

```

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4 Full investment, long only and mean return constraints

```

clist <- c("sum", "lo", "mu.target")
cset <- combine.cset(clist=clist, returns=returns, list.arg=list.arg)

```

```

## sum
## lo
## mu.target

```

```
gmv(returns, cset=cset, wts.only=T,digits=4)
```

```
## $WTS
##      MAT      EMN      LEG     AAPL      UTR
## 0.0000 0.0000 0.0000 0.3622 0.6378
##
## $MU.PORT
## [1] 0.02
##
## $SD.PORT
## [1] 0.0831
```

5 Full investment, long only, box and group constraints

```
clist <- c("sum","lo","box","groups")
cset <- NULL
cset <-combine.cset(clist=clist,returns=returns,list.arg=list.arg)
```

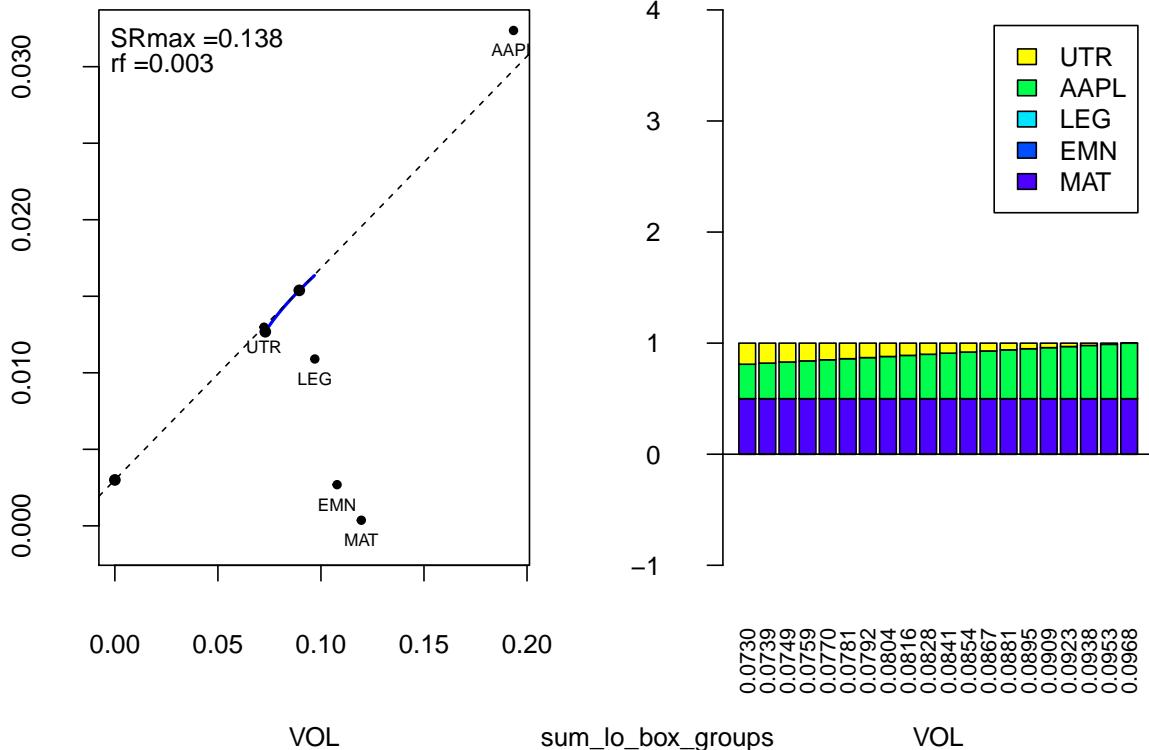
```
## sum
## lo
## box
## groups
```

```
gmv(returns, cset=cset, wts.only=T,digits=4)
```

```
## $WTS
##      MAT      EMN      LEG     AAPL      UTR
## 0.5000 0.0000 0.0000 0.1574 0.3426
##
## $MU.PORT
## [1] 0.0097
##
## $SD.PORT
## [1] 0.0657

efrontPlot(returns, cset, rf = .003, npoints = 20,wts.plot = T,
           bar.ylim = c(-1,4),list.arg=list.arg)
mtext(paste(clist,collapse=" ")),side=1,line=5)
```

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6 Full investment, long only and turnover (2 versions) constraints

```

clist <- c("sum", "lo", "turnover")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg=list.arg)

## sum
## lo
## turnover

gmv(returns, cset=cset, wts.only=T, digits=4)

## $WTS
##      MAT      EMN      LEG      AAPL      UTR
## 0.2000 0.1477 0.1544 0.1479 0.3500
##
## $MU.PORT
## [1] 0.0115
##
## $SD.PORT
## [1] 0.063

```

```

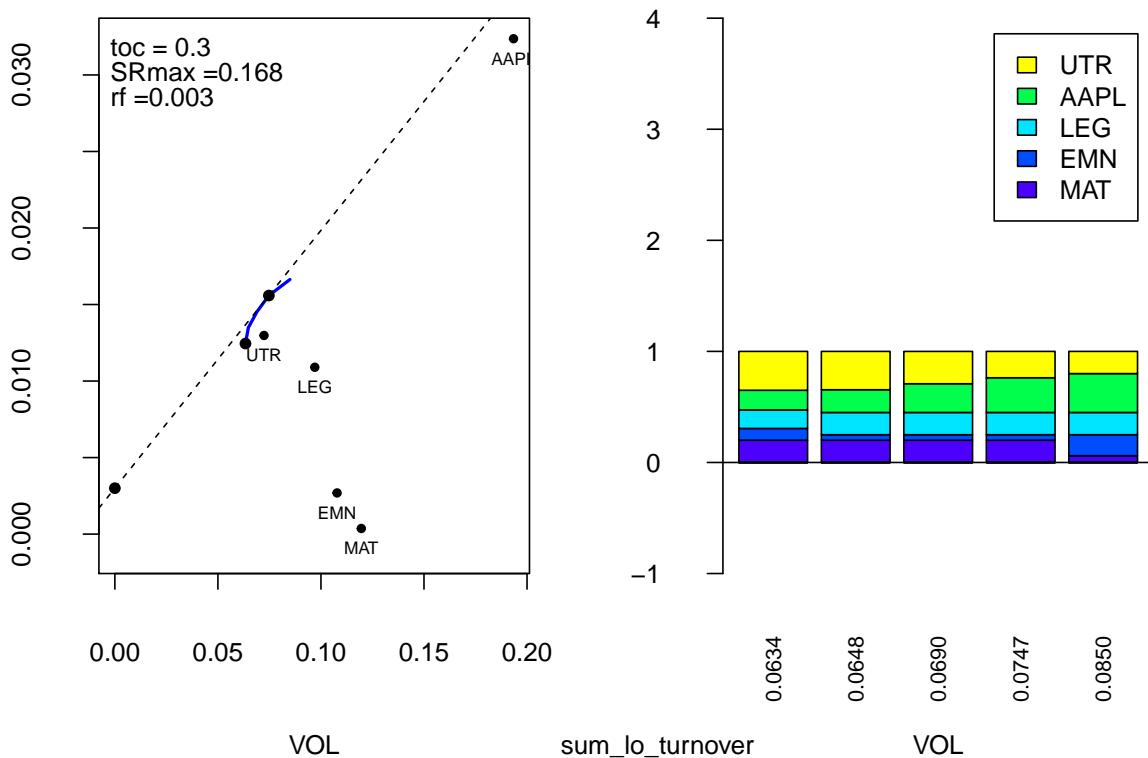
efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
           bar.ylim = c(-1,4), list.arg=list.arg)

## [1] "turnover/propcost constraints reduced the max mean return in efficient frontier plot"

mtext(paste(clist, collapse="_"), side=1, line=5)

```

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```

# 1+4+1+4+4+2+2+1+4+4+4
# sum+lo+mu.target+box+box+group+group+turnover+w.sell+w.buy+w.initial

clist <- c("sum", "lo", "turnover.doug")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg=list.arg)

## sum
## lo
## turnover.doug

gmv(returns, cset=cset, wts.only=T, digits=4)

```

```
## $WTS
```

```

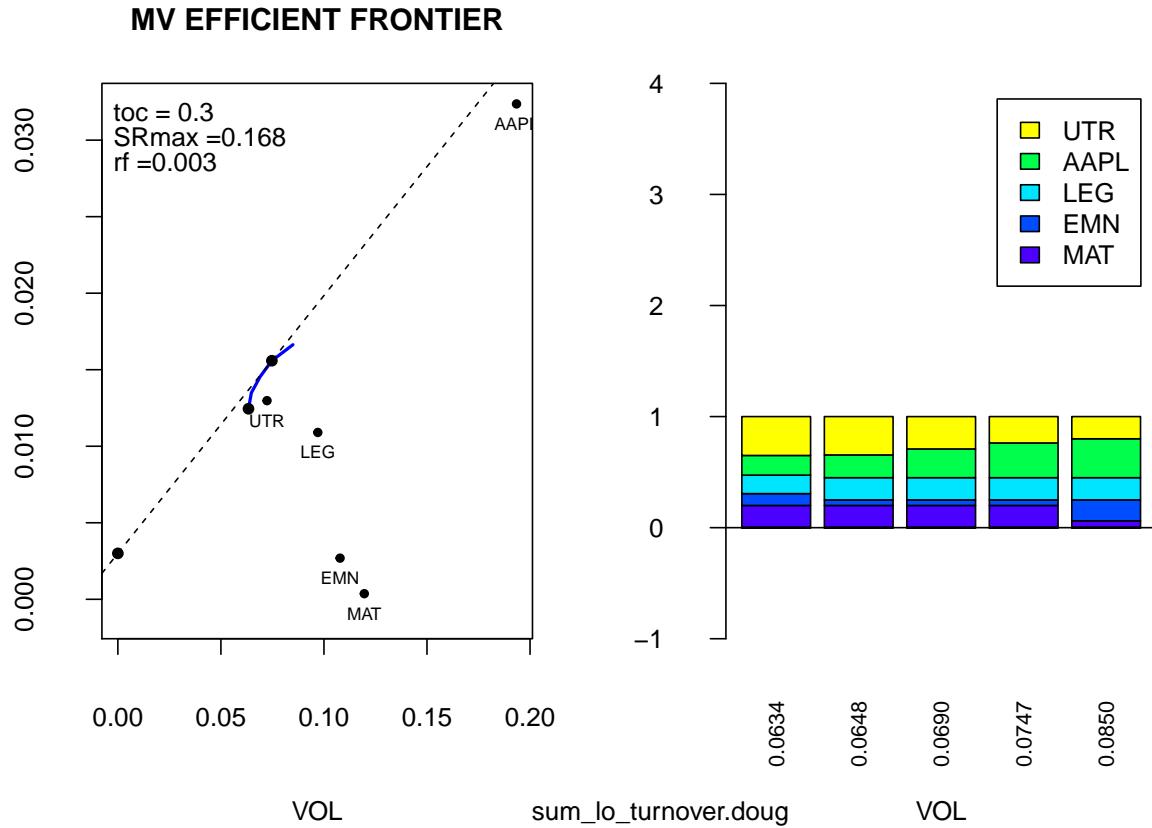
##      MAT      EMN      LEG     AAPL      UTR
## 0.2000 0.1477 0.1544 0.1479 0.3500
##
## $MU.PORT
## [1] 0.0115
##
## $SD.PORT
## [1] 0.063

efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
           bar.ylim = c(-1,4), list.arg=list.arg)

## [1] "turnover/propcost constraints reduced the max mean return in efficient frontier plot"

mtext(paste(clist,collapse="_"), side=1, line=5)

```



```

# 1+4+1+4+4+2+2+1+4+4+4
# sum+lo+mu.target+box+box+group+group+turnover+w.sell+w.buy+w.initial

```

7 Propcost constraints

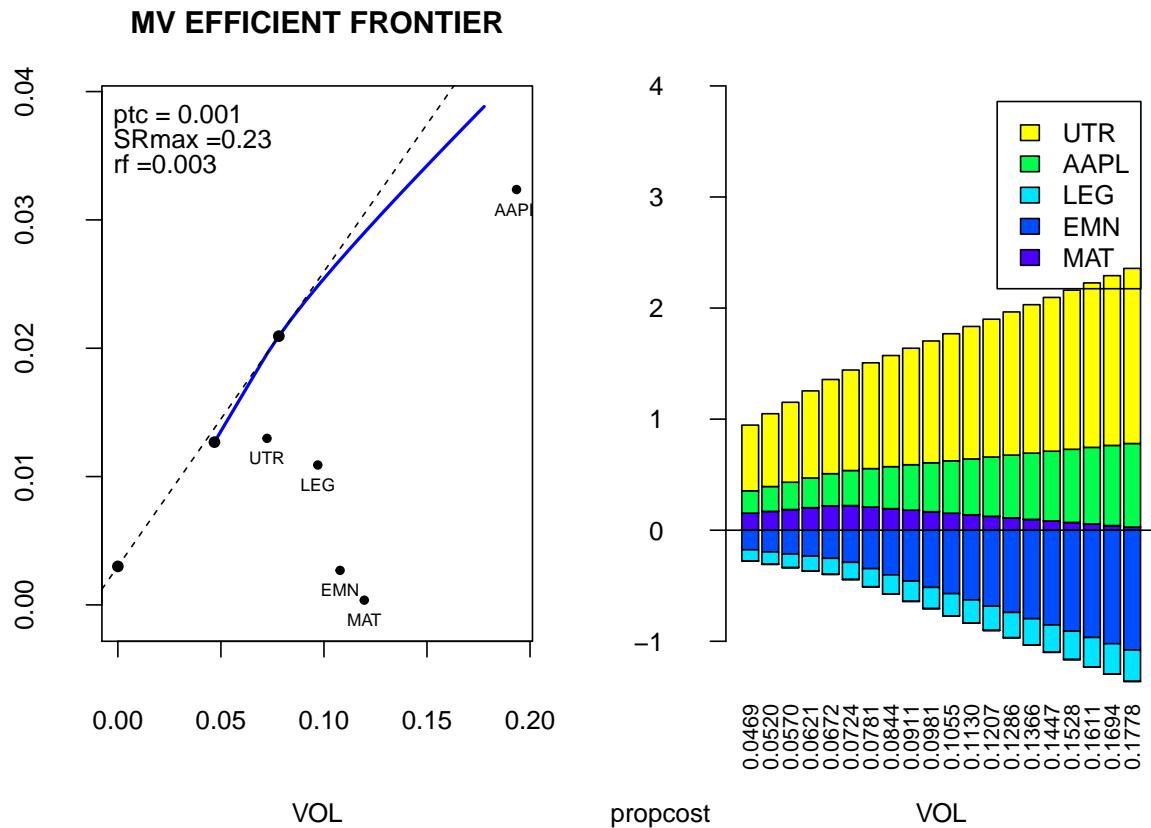
```
clist <- c("propcost")
cset <- NULL
cset <-combine.cset(clist=clist,returns=returns,list.arg)

## propcost

gmv(returns, cset=cset, wts.only=T,digits=4)

## $WTS
##   MAT   EMN   LEG AAPL   UTR
##   0     0     0     0     0
##
## $MU.PORT
## [1] 0
##
## $SD.PORT
## [1] 0

# global minum variance portfolio can always be achieved if all the initial weights are consumed by propcost
```



8 Long only and propcost constraints

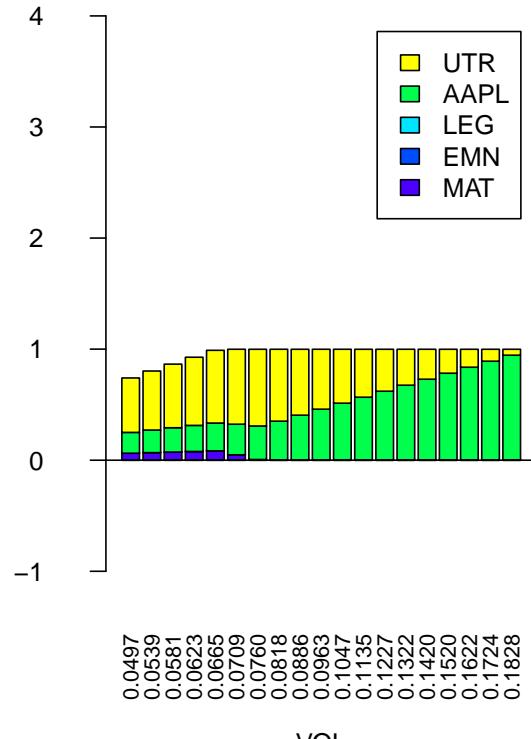
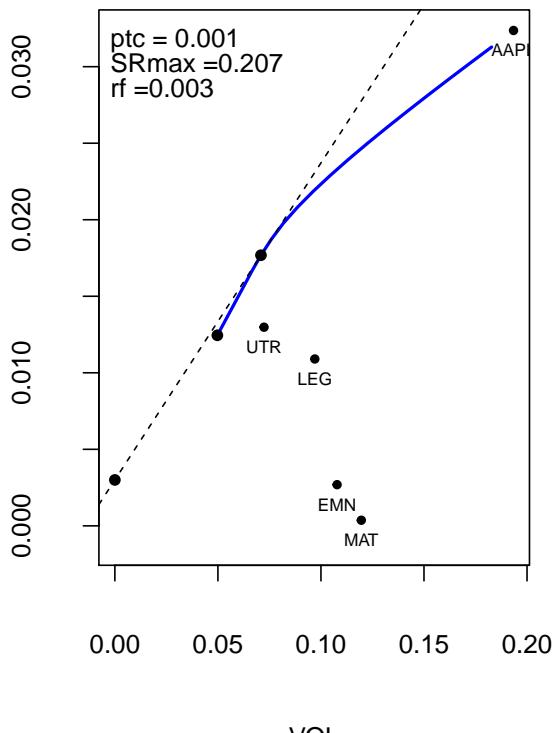
```

clist <- c("lo", "propcost")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg)

try(efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
               bar.ylim = c(-1,4), list.arg=list.arg))

```

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```
# Expected warning msg: no solution, consider relaxing constraints
```

```
## lo
## propcost

## [1] "turnover/propcost constraints reduced the max mean return in efficient frontier plot"
```

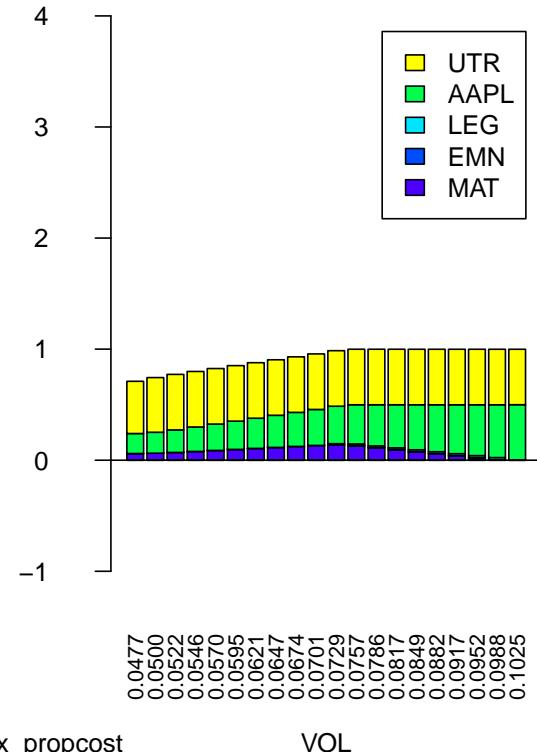
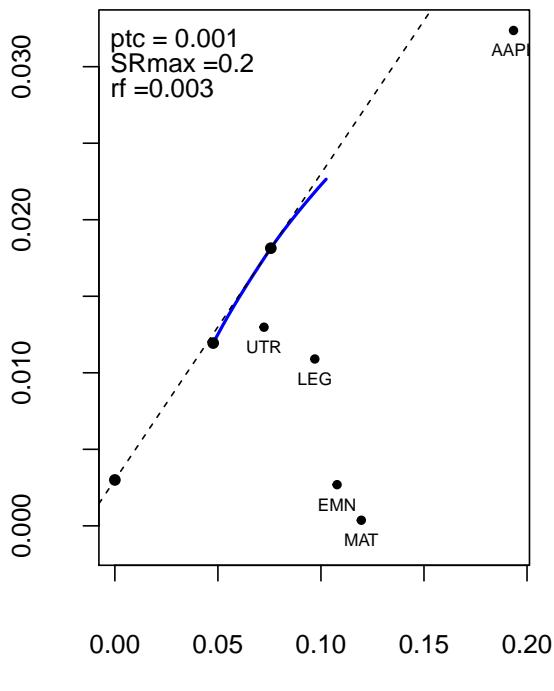
9 Box and propcost constraints

```
clist <- c("box", "propcost")
cset <- NULL
cset <- combine.cset(clist=clist, returns=returns, list.arg)
```

```
## box
## propcost

efrontPlot(returns, cset, rf = .003, npoints = 20, wts.plot = T,
           bar.ylim = c(-1,4), list.arg=list.arg)
mtext(paste(clist, collapse="_"), side=1, line=5)
```

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10 Sum, box and propcost constraints (Bad example, expecting errors)

```
clist <- c("sum", "box", "propcost")
list.arg <- list( sum=sum,
                  upper=upper,
                  lower=lower,
                  ptc=ptc,
                  w.initial=w.initial)
print(list.arg)
```

```
## $sum
## [1] 1
##
## $upper
## [1] 0.5 0.5 0.5 0.5 0.5
##
## $lower
## [1] 0 0 0 0 0
##
```

```
## $ptc
## [1] 0.001
##
## $w.initial
## [1] 0.2 0.2 0.2 0.2 0.2

cset <- NULL
cset <-try(combine.cset(clist=clist,returns=returns,list.arg))

## sum

# Expected error msg: Error in propcost.modify(cset.i) :
# sum constraint are not combinable with propcost constraint
```